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3	Skill of the MJO and Northern Hemisphere Blocking
4	in GEFS Medium-Range Reforecasts
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8	Thomas M. Hamill and George N. Kiladis
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12	NOAA Earth System Research Lab
13	Physical Sciences Division
14	Boulder, Colorado, USA
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18 19	Submitted to Monthly Weather Paying
20	Submitted to Monthly Weather Review
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22	14 June 2013
23	11 Julie 2015
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31	Corresponding author address:
32	
33	Dr. Thomas M. Hamill
34	NOAA Earth System Research Lab, Physical Sciences Division
35	R/PSD1, 325 Broadway
36	Boulder, Colorado USA 80305-3328
37	e-mail: tom.hamill@noaa.gov
38	phone: +1 (303) 497-3060 telefax +1 (303) 497-6449
39	

#### ABSTRACT

Forecast characteristics of Northern Hemisphere atmospheric blocking and the MJO were diagnosed using an extensive time series (Dec-Jan-Feb 1985-2012) of daily medium-range ensemble reforecasts based on an approximately stable version of the NCEP Global Ensemble Forecast System (GEFS).

For blocking: (a) the GEFS slightly under-forecasted blocking frequency at longer leads in the Euro-Atlantic sector, and inter-annual variability of blocking frequency was quite large; (b) predictive skill of actual blocking was substantially smaller than its perfect-model skill; (c) block onset and cessation were forecast less well than overall blocking; (d) there was substantial variability of blocking skill between half-decadal periods; and (e) the reliability of probabilistic blocking forecasts degraded with increasing lead time.

For the MJO: (a) forecasts of strong MJOs propagated too slowly, especially the component associated with outgoing longwave radiation (OLR), i.e., convection; (b) tropical precipitation was greatly over-forecast at early lead times; (c) the ensemble predictions were biased and/or under-dispersive, manifested in U-shaped rank histograms of MJO indices. Magnitude forecasts were especially U-shaped. (d) bi-variate MJO correlation skill was larger for its wind than for its OLR component, and was larger for the higher-amplitude MJO events; (e) there was some half-decadal variability in skill; (f) probabilistic skill of the MJO forecast was modest, and skill was larger when measured relative to climatology than when measured relative to a lagged persistence forecast.

For longer-lead forecasts, the GEFS demonstrated little ability to replicate the changes in blocking frequency due to a strong MJO that were noted in analyzed data.

#### 1. Introduction.

(Straub 2013).

Medium-range predictability and forecastability¹ of low-frequency modes of atmospheric variability can be evaluated more readily with a long time series of forecasts. In this manuscript we evaluate two such modes of variability, Northern Hemispheric atmospheric blocking and the Madden-Julian Oscillation (MJO; Madden and Julian 1971) and their interactions using an extensive set of global medium-range ensemble reforecasts.

Both the MJO and blocking occur somewhat infrequently at a particular location. Using the blocking definition of Tibaldi and Molteni (1990), Northern Hemisphere wintertime blocking occurs approximately 2% to 22% of the time, averaged over several decades. Blocks are most common over the eastern Atlantic Ocean and western Europe, with a secondary frequency maximum in the central Pacific Ocean. Blocks can be persistent, leading to both long periods of rather similar, and often high-impact weather. For the slowly moving, large-scale, equatorially trapped tropical convective clusters and associated wind perturbations

<sup>1</sup> Predictability here refers to an intrinsic property of the atmospheric process and measures the time scale at which two initially similar but not identical perturbed initial conditions will become as different as random draws of atmospheric states. While numerical models are often used to estimate the (unknown) predictability, the predictability is not a forecast property. Forecastability, in contrast, indicates the ability of the forecast model to provide guidance that the user will judge to have some value. Forecastability may be evaluated with many different metrics.

known as the MIO, a given year may produce only a couple coherent, high-amplitude

MJO events, although this number will vary depending on the definition of the MJO

Evaluating the predictability and forecastability of blocking and the MJO are challenging given the infrequency and the temporal continuity of these events, the latter of which reduces the effective sample size (Wilks 2006, eq. 5.12). If one is interested, for example, in the ability of the model to forecast block onset for a particular longitude band, a three-month period may have, say, 15 days with blocked conditions, but most likely those 15 days occurred in 1-3 persistent blocking events. Similar issues occur with the MJO. The interaction of two such events is even more difficult to evaluate with limited samples, e.g., evaluating the change in blocking frequency related to a large forecast MJO event in the Indian Ocean. A large sample size could be provided from a reforecast, i.e., a multi-year or preferably a multi-decadal sample of forecasts from a fixed forecast model and assimilation system.

Extensive reforecasts (hindcasts) often haven't been available to facilitate such studies. For blocking, the most comprehensive recent study was by Jung et al. (2012), which used hindcasts to document blocking frequency in extended-range simulations from the European Centre for Medium-Range Weather Forecasts (ECMWF) model at various resolutions. The authors found that Euro-Atlantic sector blocking frequency was generally more under-forecast with lower-resolution models. Older studies included the Watson and Colucci (2002) study of Northern Hemispheric wintertime blocking using data from the operational NCEP global spectral model from 1995-1998, and Mauritsen and Källén (2004), who studied blocking in the ECMWF system during the Northern Hemispheric 2000-2001 winter. Both studies found too few blocks in the forecast. Pelly and Hoskins (2003a), using

a potential vorticity-based method of defining blocks, evaluated the ECMWF output for a year of data beginning on 1 August 2001, a period spanning several model changes. Though they also found blocking frequency was under-forecast, there was positive skill in the probabilistic forecasts of blocks out to 10 days, and they found block onset was better forecast than block cessation.

There have been more recent studies of the MJO than for blocking, for seasonal simulations at least. The MJO is being actively studied in part because it affects monsoon (Yasunari 1979) and tropical cyclone variability (Maloney and Hartmann 2000ab). The MJO also can excite extra-tropical Rossby wave trains (Knutson and Weickmann 1987, Jones et al. 2004, Weickmann and Berry 2009) and can interact with mid-latitude, low-frequency modes of variability such as the North Atlantic Oscillation (Lin et al. 2009). The MJO is often poorly forecast, and there is some evidence that an improved MJO forecast may result in improved mid-latitude forecasts (Ferranti et al. 1990, Vitart and Molteni 2010).

The interaction of the MJO with the mid-latitude flow and its forecastability has been an active area of investigation (Leibmann and Hartmann 1984, Kiladis and Weickmann 1992, Hendon et al. 2000; Riddle et al. 2012). Since the MJO represents the variability at time scales of 30-70 d<sup>-1</sup>, (e.g., Waliser et al. 2009), it has been common to examine numerical simulations to lead times of several months and to leverage hindcasts to provide large-enough samples. Examples of studies with seasonal forecast models and hindcasts include Hendon et al. (2000), Lin et al. (2008), Seo et al. (2009), Kim et al. (2009), Vitart and Molteni (2010), Gottschalck et al. (2010), Kang and Kim (2010), Jia et al. (2010), and Crueger et al. (2013). For the

medium range (here, roughly +3 to +16 days lead time), the literature on MJO forecast evaluation is sparser. Some verification statistics were calculated for THORPEX Interactive Grand Global Ensemble (TIGGE; Bougeault et al. 2010) data by Matsueda and Endo (2011).

Recently, NOAA scientists created an extensive global ensemble reforecast data set (Hamill et al. 2013) using the version of the NCEP Global Ensemble Forecast System (GEFS) that was operational in 2012-2013. This data set was created to facilitate the diagnosis and statistical correction of systematic forecast errors in medium-range ensemble forecasts, thereby improving GEFS guidance. In this article, we demonstrate an ancillary purpose, showing how the extensive reforecasts facilitate the diagnosis of errors in low-frequency modes of variability. Specifically, we will examine the usefulness of the reforecasts for examining the predictability and forecastability of blocking and the MJO as well as their inter-relationships. The operating hypothesis, which as we will show is easily disproved, is that the ensemble prediction system well represents the evolution of forecast uncertainty of these phenomena.

Below, section 2 briefly describes the data set and the methods for forecast evaluation. Section 3 provides results, while section 4 provides a discussion and conclusions.

## 2. Data and Methods

a. Description of the data sets.

Unless noted otherwise, reforecast data for Dec-Jan-Feb 1985-2012 period was used in this study. The global ensemble reforecast data was more completely described in Hamill et al. (2013). Briefly, this reforecast data set is based on the 2012 version of the NCEP Global Ensemble Forecast System (GEFS). An 11-member retrospective ensemble forecast was generated to +16 days lead for every day at 00 UTC from 1 December 1984 to the current date. Consistent with the operational GEFS, the model resolution was T254L42 to day +8 ( $\sim$ 40-km grid spacing at 40 $^{\circ}$ latitude and 42 levels). Starting at day +7.5 and extending to day +16, the reforecasts were conducted at the reduced resolution of T190L42 (~54-km grid spacing). Through 20 February 2011, the Climate Forecast System Reanalysis (CFSR; Saha et al. 2010) provided the control initialization and verification. Thereafter, the operational grid-point statistical interpolation (GSI; Kleist et al. 2009) procedure was used, which was updated to a hybrid variational-ensemble data assimilation approach (Hamill et al. 2011) on 22 May 2012. Additional ensemble member perturbed initial conditions were generated using the ensemble transform with rescaling approach of Wei et al. (2008). See Hamill et al. (2013) for more details on the data set, including a description of the extensive amount of data that is available for fast-access download. In this study, data interpolated to a 1degree grid was used. For examination of associated tropical precipitation forecasts, 1-degree Global Precipitation Climatology Project (GPCP, Huffman et al. 2001) data was used.

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This GPCP data was available only from 1997 – current.

### b. Blocking and MIO definitions.

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For blocking, though there have been some modern alternatives (e.g., Pelly and Hoskins 2003b, Barnes et al. 2012), here blocking was defined directly following the simple method of Tibaldi and Molteni (1990) based on 500 hPa geopotential heights. Conditional climatologies of blocked and unblocked 500 hPa height patterns at the international dateline are shown in Fig. 2. Given the increased frequency of blocking in the Euro-Atlantic and Pacific regions (Fig. 2a), our analysis of blocking forecastability and predictability was limited to two sectors, the "Euro-Atlantic" sector, from 45° W longitude to 45° E longitude, and the "Pacific" sector, from 140° E longitude to 130° W longitude. For MJO analysis, a now-standard method was used to compute the projections onto the two leading empirical orthogonal functions (EOFs) of MJO variability (Wheeler and Hendon 2004; hereafter WH04). The respective EOFs are commonly known as "RMM1" and "RMM2." The EOF structures associated with RMM1 and RMM2 were taken directly from the real-time MJO web site, http://cawcr.gov.au/staff/mwheeler/maproom/RMM/. The EOFs were computed from a time series of longitudinal arrays of filtered anomalies in the 200 and 850 hPa zonal winds and outgoing longwave radiation (OLR), which were averaged in the band from 15° S to 15° N latitude and normalized by their variances over this latitude band and all longitudes. This filtering also removed inter-annual variability and the projection onto the El Niño/Southern Oscillation (ENSO). The processing of the reforecast data to calculate the projections of forecast data onto RMM1 and RMM2 generally followed the procedure outlined by WH04, with the following

exception. To remove the effects of ENSO, the projection of the filtered data onto the Niño 3.4 index anomalies was removed (Trenberth 1997), as opposed to the "SST1" index of Drosdowsky and Chambers (2001) cited in WH04. The filtering did remove the leading three harmonics of the annual cycle and the mean of the previous 120 days, as in WH04. Our procedure, when applied to the control initial condition from the CFSR, produced a time series of projections that was a very close match to the time series produced by WH04 with NCEP-NCAR reanalyses (Kalnay et al. 1996) data (not shown).

### c. Methods of forecast evaluation.

Many methods were used to evaluate blocking and MJO forecast skill. For blocking, a Brier Skill Score was used that measured the skill of the ensemble forecast's ability to set forecast probability of blocked conditions. The Brier Score of the forecast and climatology were computed separately for each longitude in the standard manner (Wilks 2006, eq. 7.34). The Brier Skill Score (BSS; ibid, eq. 7.35) was computed from the sums of Brier Scores of the forecast and climatology over each longitude within a sector. Forecast probabilities of blocking were set directly by ensemble relative frequency. For example, if 3 of the 11 members were diagnosed as having blocked conditions at a particular longitude, the forecast probability was set to 3/11. Since climatological blocking frequency did not vary radically within each sector (see Fig. 2 below), there was little reason to apply more complex procedures (e.g., Hamill and Juras 2006) to account for variations in climatological event frequency for each sector when calculating the BSS. Skill will

also be evaluated for block onset and cessation for long-lived blocks. The subset of dates classified as "block onset" for long-lived blocks were those dates where, within a given sector, there were < 20 degrees of longitude that were blocked the day before but  $\geq$  20 degrees blocked on that day, and where  $\geq$  20 degrees continued to be blocked for at least the subsequent 9 days. Dates classified as "block cessation" were those dates where, for the first date after a defined block onset, < 20 degrees of longitude were blocked. Finally, we will also evaluate the BSS of a "perfect-model" forecast (Buizza 1997). One of the 11 forecast members replaced the analyzed state, and then the existence / non-existence of a block was computed from this replacement data. Probabilities were estimated from the diagnoses of blocking from the remaining 10 forecast members.

Reliability diagrams (Wilks 2006, p. 287) for blocking probabilities were also calculated in the standard manner.

The MJO was also evaluated with a variety of metrics. Following now standard metrics defined by Lin et al. (2008), the correlation skill (COR) and root-mean-square error (RMSE) of the RMMs were calculated over all ensemble members as:

$$COR(\tau) = \frac{\sum_{j=1}^{11} \sum_{i=1}^{N} \left[ RMM1_{i}^{a} RMM1_{ij}^{f} + RMM2_{i}^{a} RMM2_{ij}^{f} \right]}{\sqrt{\sum_{j=1}^{11} \sum_{i=1}^{N} \left[ RMM1_{i}^{a^{2}} + RMM2_{i}^{a^{2}} \right]} \sqrt{\sum_{j=1}^{11} \sum_{i=1}^{N} \left[ RMM1_{ij}^{f^{2}} + RMM2_{ij}^{f^{2}} \right]}}$$
(1)

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$$RMSE(\tau) = \sqrt{\frac{1}{Nx11}} \sum_{j=1}^{11} \sum_{i=1}^{N} \left\{ \left[ RMM \mathcal{I}_{i}^{a} - RMM \mathcal{I}_{ij}^{f} \right]^{2} + \left[ RMM \mathcal{I}_{i}^{a} - RMM \mathcal{I}_{ij}^{f} \right]^{2} \right\}$$
(2)

where  $\tau$  is the lead time in days,  $RMM1_i^a$  and  $RMM2_i^a$  are the analyzed RMM1 and RMM2 projections for the ith of N sample days.  $RMM1_{ij}^f$  and  $RMM2_{ij}^f$  are their respective, time-concurrent forecast projections for each of the jth of 11 members. The COR and RMSE will also be calculated for "high-amplitude" and "low-amplitude" events. The ith forecast sample is evaluated as high amplitude or low amplitude depending on the magnitude of the associated analysis. The sample is high amplitude if  $\sqrt{[RMM1_i^a + RMM2_i^a]^2} \geq 1.0$  and low amplitude if < 1.0.

We were also interested in the ability of the ensemble to provide high-quality, reliable probabilistic guidance. For the MJO, reliability (or more accurately, "consistency") was evaluated with rank histograms (Hamill 2001). Rank histograms were calculated separately for RMM1 and RMM2, but the average of the two is reported. Rank histograms were also generated for MJO phase and amplitude. In generating the rank histograms, the observed value of RMM1 and RMM2 were assumed to be perfect, so no noise was introduced to ensemble members to potentially account for inaccuracies in the analyses of RMMs (ibid, Fig. 6 therein). The phase and amplitude propagation characteristics of the reforecasts will also be examined; the specific methodology for these will be discussed at the relevant point in the results section.

A continuous ranked probability skill score (CRPSS; Wilks 2006, p. 302) was also calculated for MJO forecasts against two reference forecasts, climatology and lagged persistence. As with rank histograms, continuous ranked probability score (CRPS) statistics for the forecast and the reference were calculated separately for RMM1 and RMM2 and then summed. Let  $\Phi_i^f$  represent the ensemble forecast

- cumulative distribution function (CDF) for RMM1 or RMM2 for the ith of N samples.
- Similarly, let  $\Phi^a_i$  represent the analyzed CDF, which is a step function, 0 below the
- 266 RMM value and 1 above.  $\Phi_i^r$  is the CDF of the reference forecast, be it the
- 267 unconditional climatology for Dec-Jan-Feb or a lagged persistence forecast. Then
- the CRPSS was calculated as

$$CRPSS = 1.0 - \frac{CRPS^f}{CRPS^r} \qquad , \tag{3}$$

- where the *CRPS f* was the continuous ranked probability score (CRPS) of the forecast
- and *CRPS* <sup>r</sup> was the CRPS of the reference. *CRPS* <sup>f</sup> was calculated via

$$CRPS^{f} = \frac{1}{N} \sum_{i=1}^{N} \int_{RMM=-\infty}^{\infty} \left( \Phi_{i}^{f} - \Phi_{i}^{a} \right)^{2} dRMM \qquad , \tag{4}$$

- with the *CRPS* <sup>r</sup> calculated similarly. For the climatological reference forecast, a
- Gaussian distribution was fitted to the climatology individually for RMM1 and
- 275 RMM2, which was then used to generate the CDFs. The lagged persistence was
- based directly on the "PCRLAG" approach documented in Seo et al. (2009, their eq.
- 277 1). Future RMM values were predicted using a multiple linear regression model
- using the current RMM values and their values 5, 10, 15, 20 and 25 days in the past.
- Some figures below will include PDFs of the daily change in the angle  $\theta$  and
- magnitude of RMM in the (RMM1, RMM2) phase space.  $\theta$  measures the rotation
- from the positive RMM1 axis, and is defined as

$$\theta = tan^{-1}(RMM2/RMM1), \tag{5}$$

- 283 which can be defined uniquely in the interval  $-180^{\circ} \le \theta < 180^{\circ}$  with knowledge of
- the signs of RMM2 and RMM1. Angles of -180° to -135° correspond to "phase 1" in
- the (RMM1, RMM2) phase space (see Wheeler and Hendon 2004, Fig. 7); angles of -

 $135^{\circ}$  to  $-90^{\circ}$  correspond to "phase 2," and so on. The PDFs of  $\theta$  and RMM magnitude were estimated with kernel density estimation using a Cressman-shaped kernel (Cressman 1959) that tapered to 0.0 at  $2^{\circ}$  or 0.1 units of RMM magnitude.

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## 3. Results.

a. Blocking forecasts.

Figure 2a shows the blocking frequency in the GEFS reforecasts for selected forecast lead times. Overall, the GEFS replicated blocking frequency reasonably accurately, though for lead times of +6 days and beyond it under-forecasted blocking frequency in the Euro-Atlantic sector by up to 25%. While the blocking frequency curves are relatively smooth over the multi-decadal period, this disguises tremendous inter-annual variability. Figure 2b shows the yearly blocking frequencies, spatially smoothed slightly to aid in interpretability. For a given longitude, blocking frequencies can vary by an order of magnitude or more from one year to the next. Figure 3 shows that overall positive blocking forecast skill was retained through day +13, but this skill was far short of the skill that was possible under-perfect model assumptions. For example, the perfect-model skill at day +7 was as large as the actual skill at  $\sim$  day +3.5. It is somewhat likely that the perfectmodel estimate of forecast skill is somewhat too large, too, due to the tendency for the ensemble forecasts to cluster together, such that their spread is not statistically consistent with their ensemble-mean error (e.g., Bougeault et al. 2010, Figs. 2-3). Figure 3 also shows that blocking onset and cessation were somewhat less well forecast than the overall forecasts of blocking. The skill curves for onset and

cessation were noisier because of the greatly reduced sample size, even with 28 winter seasons of data. Figure 4 shows that there was a substantial amount of variability in the skill of blocking when the data was sorted by half-decadal periods, plus 2010-2012. In the Pacific sector, the blocking skill in the most recent 3 years was the largest, but the 2005-2009 period was intermediate in skill and actually comparable to the skill during the 1985-1989 period. However, in the Euro-Atlantic sector, the skill for the 1985-1989 period was substantially smaller than for the subsequent half decades. The dashed lines in Fig. 4 provide the half-decadal skill results under the perfect-model assumption. These show some natural variability in skill at half-decadal timescales. Note that the 1985-1989 period, for example, had the lowest perfect-model predictability in the Euro-Atlantic sector, which probably contributed to its especially low real-model skill, while the 2010-2012 period had among the highest perfect-model skill in the Pacific, indicating that the actual high forecast skill for this period was in part natural variability. The perfect-model results here also suggest that even in the best of circumstances, blocking forecast skill as defined here is limited to approximately two weeks.

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Figure 5 presents reliability diagrams for the blocking forecasts at various lead times. At the earlier lead times the blocking forecasts are mostly reliable, but the reliability decreases so that by day +15 the forecasts are rather unreliable. As expected, blocking forecast sharpness decreases over time, as seen in the usage frequency histograms. There are probably many reasons for the lack of reliability, including all the usual suspects with unreliable ensemble forecasts; the moderate resolution of the forecast model, the deficiencies in parameterizations, including

sometimes inappropriate deterministic formulations (Palmer 2012), the suboptimal initialization of both the control and perturbations in the ensemble system, and, as we shall see below, faulty representations of interactions with the MJO.

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# b. MJO forecasts.

Figure 6 shows the evolution from both analyzed and deterministic forecasts where the vector (RMM1, RMM2) of initial conditions was within 0.5 units of (1.5, -1.5), i.e., within the purple circle on the figure. The samples are all various dates from Dec-Jan-Feb 1985-2012. It appears that the collection of forecasts propagate somewhat more regularly than the collection of analyzed states, and perhaps the forecasts lose some amplitude. Figures 7 and 8 attempt to quantify this, providing a PDF of the daily change in overall RMM angle and magnitude, respectively, as well as the change attributable specifically to wind and OLR components of the RMM. The cases used to populate Figs. 7 and 8 were selected in an attempt to isolate situations where there was a real MIO between Africa and the Maritime continent, and where it had robust associated convection. Consequently, only the Dec-Jan-Feb 1985-2012 cases that were included were those that had an RMM amplitude of greater than 1.0. an RMM2 < 0.0, and an OLR contribution to the RMM amplitude of greater than 0.5 were included. Consider the overall phase change in Fig. 7a; after a reasonable mean phase change the first day, for subsequent leads the mean phase change was substantially smaller for the forecast than for the analyzed, with a phase change of 5-10° for the analyzed but 3-6° for the forecast. Forecast MJOs propagated too slowly, on average. The forecast propagation of the OLR component of RMM was

slower than the wind component, though this was true to a lesser extent with analyzed data as well. This slower propagation can also be diagnosed, for example, from the reanalyzed rainfall and wind lag correlations shown in Fig. 3 from Weaver et al. (2011). By inspection, the distributions of phase changes of the forecast PDFs were not dramatically narrower than of the analyzed PDFs; the main deficiency was a biased mean, not a lack of spread. Considering the overall magnitude change in Fig. 8a, both forecast and analyzed exhibit a similar small decrease in magnitude, though the PDF for the forecast appears slightly more narrow and peaked than for the analyzed.

Not only did the forecast MJO precipitation features propagate too slowly, but also the precipitation forecasts exhibited significant bias (Fig. 9). Precipitation amounts were dramatically over-forecast at the early forecast leads. The general pattern of the daily GPCP precipitation amount climatology was reasonably replicated in day +0 to 1 forecast (Fig. 9b), but the average daily forecast precipitation amounts was commonly > 50% too large. By the beginning of the second week of the forecast (Fig. 9c), the over-forecast bias was reduced, but there was less resemblance with the analyzed precipitation pattern. For example, the connection of the South Pacific Convergence Zone (SPCZ; Folland et al. 2002) to the inter-tropical convergence zone was missing, and the forecast SPCZ was unduly zonally oriented, as it often is in climate simulations (Brown et al. 2011). These pattern changes were even more evident at the end of week +2 (Fig. 9d).

An additional deficiency of the probabilistic MJO forecasts was their underdispersion and/or conditional bias. This can be seen by examining the rank histograms from the ensemble predictions of MJO RMMs (Fig. 10). All of the rank histograms were U-shaped, which was most pronounced for the short-lead RMM amplitude forecasts. The rank histograms indicate that there was unrealistic consistency of magnitudes among the forecasts; the ensemble prediction system did not adequately simulate the forecast processes that contribute to diversity in MJO magnitudes.

Despite the significant biases, the forecasts still exhibit skill in the first week. Figure 11 presents the CRPSS of the forecasts measured relative to an unconditional climatology and relative to the regression-based lagged persistence model. The lagged persistence model presented a tougher reference standard, so forecasts exhibited less skill in comparison to this. Skill diminished to near 0 by day +11 with respect to lagged persistence and by day +14 with respect to climatology. While lagged persistence represented a tougher reference, we note that the first-generation Climate Forecast System at NCEP (Wang et al. 2005, Saha et al. 2006) produced forecasts that had higher errors and less correlation skill than the lagged persistence at all forecast leads. Thus, the current GEFS provides substantial improvement in the simulation of the MJO relative to the first-generation CFSR.

Consider now the correlation skill and RMSE of MJO forecasts (Fig. 12).

Overall correlation skill and RMSE were comparable to those from the more accurate models shown in Matsueda and Endo (2011). There was more correlation skill in the wind components of the RMM than in the OLR component, as shown in Fig 12(a). This likely relates to the better ability of models to maintain and evolve the rotational component of the wind over the area of convection, perhaps due to

improved initial conditions. The correlation skill was much lower for the first two half-decadal periods, 1985-1989 and 1990-1994, than for the subsequent periods, with the exception of 2010-2012, though the RMS error was not larger for the first decade of the forecast (Figs. 12 (c) and (d)). Figures 12 (e) and (f) show that forecasts initialized from analyses with high amplitude of RMM exhibited more skill but also higher RMSE than lower-amplitude forecasts. This was also shown in Lin et al. (2008, their Fig. 13),

c. Interactions between blocking and the MJO.

Finally, we briefly consider the ability of the forecast model to successfully replicate the ability to discern changes in blocking frequency for different phases of strong MJOs. Strong MJOs are defined as the set of dates where the magnitude of the RMM is in the upper quartile of its distribution, forecast or observed. Figure 13 presents the results. Consider panel (a). Here the change in blocking frequency for a strong MJO relative to the unconditional blocking frequency is shown as a function of longitude (abscissa) and of the analyzed phase  $\theta$  (ordinate) of the MJO, as defined in section 2c. To provide an adequate sample size for a given  $\theta$ , the data plotted for a given  $\theta$  actually includes analyzed samples with similarly diagnosed  $\theta$ , specifically where -22.5°  $\leq \theta \leq$  22.5°. Note some interesting characteristics in the analyzed relationship of blocking frequency changes. As  $\theta$  varies between 0° and 120° (i.e., the MJO's center moves from the Maritime continent to western N. America), at 0° longitude, the blocking frequency changes from a strongly negative anomaly in blocking frequency to a strongly positive anomaly. Restated, analyzed Euro-Atlantic

blocking frequency changes from below its long-term average to above average as the MJO moves east from the Maritime continent. We note that this is consistent with previous results, such as the 500 hPa anomaly composite for various phases of the MJO in Lin et al. (2009, Fig. 4). Our figure 13(b)-(d) then show the respective blocking frequency anomalies when the *forecast* MJO phase is of the noted angle, and when the *forecast* MJO magnitude is greater than the upper quartile of the forecast distribution. The day +4 forecast in panel (b) still replicates many of the essential anomalies of the analyzed, including the shift from a strongly positive blocking frequency anomaly to a strongly negative anomaly along the Greenwich meridian as  $\theta$  varies between 0 and 120 degrees. However, much of the frequency anomaly detail is lost by day +8, and the day +16 forecasts show no apparent relation to the analyzed. From this, we can conclude that the internal dynamics of the GEFS do not represent very well the processes that lead to inter-relationships between blocking and the MJO.

### 4. Discussion and conclusions

Some modes of atmospheric variability are uncommon enough and/or operate on long-enough timescales that a short time series of past forecasts will not prove sufficient for diagnosing their characteristics. Atmospheric blocking and the MJO are two such phenomena. In this paper we have shown how a very long time series of ensemble forecast guidance facilitates a greater understanding of the forecastability and predictability of these phenomena. In this case, the long time series was provided by a 28-year data set of reforecasts from the NCEP Global

Ensemble Forecast System. The paper more specifically explored Northern Hemispheric blocking, the MJO, and their interaction during Dec-Jan-Feb 1985-2012 period.

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With regards to blocking, the reforecasts showed that the GEFS slightly under-forecasted blocking frequency at longer leads in the Euro-Atlantic sector. Furthermore, the inter-annual variability of blocking frequency was shown to be quite large, demonstrating how difficult it can be to achieve a representative sample with only a few years of data. The predictive skill of the probabilistic forecasts of actual blocking was substantially smaller than its perfect-model skill, whereby a member of the ensemble was used as a synthetic verification. This indicates that there is still tremendous potential for improvement in blocking forecasts. However, it is also likely that the perfect-model results present a somewhat over-optimistic estimate of the upper range of forecast skill. The GEFS system and most other ensemble systems are under-dispersive, and as such, the members of the ensemble unduly resemble each other, inflating the perfect-model skill estimates. It was also found that block onset and cessation were forecast somewhat less well than block maintenance, and there was substantial variability of blocking skill between halfdecadal periods. Finally, the reliability of probabilistic blocking forecasts degraded with increasing lead time, and as expected, blocking forecasts became progressively less sharp, i.e., forecast probabilities were less often 0.0 and 1.0 and more often resembled the model climatology.

Forecasts of strong MJOs propagated too slowly, especially the component associated with outgoing longwave radiation (OLR), i.e., convection. Deep tropical

convection appeared to have other systematic biases in the GEFS; in general, there was too much tropical precipitation forecast in the Indian and Pacific Oceans, especially for the shorter forecast leads. The ensemble predictions were biased and/or under-dispersive, manifested in U-shaped rank histograms of MJO indices. Forecasts of the magnitude of the MJO's leading EOFs were especially U-shaped. Bivariate MJO correlation skill was found to be larger for the wind component than for OLR component, and skill was larger for the higher-amplitude MJO events. Skill varied significantly between half-decadal periods, with the period 1985-1994 and 2010-2012 exhibiting lower MJO skill than the 1995-2009 period. Probabilistic skill of the MJO forecast was modest, and skill was larger when measured relative to climatology than when measured relative to a lagged persistence forecast. Finally, for longer-lead forecasts, the GEFS demonstrated little ability to replicate the changes in blocking frequency due to a strong MJO that were noted in analyzed data.

This paper has discussed forecast skill without providing analysis of the potential forecast systematic errors that may lead to deficiencies in blocking, the MJO, and their inter-relationships. This much more challenging work is left as future research. We do hope that we have laid out a first step, demonstrating the predictability and forecastability of these phenomena using the newly created GEFS reforecast data set.

### **Acknowledgments:**

The reforecast data set used here was created under a 2010 Department of Energy

Advanced Leadership Computing Challenge supercomputer grant. This manuscript

493 was partly supported by a NOAA USWRP grant on methods for estimating model
494 uncertainty. We thank John Cortinas, the NOAA program manager, for his assistance
495 and guidance on USWRP.
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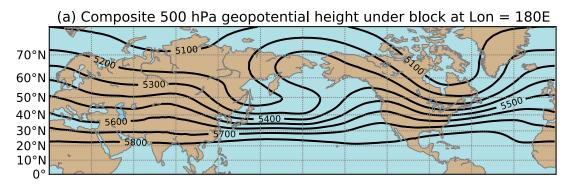
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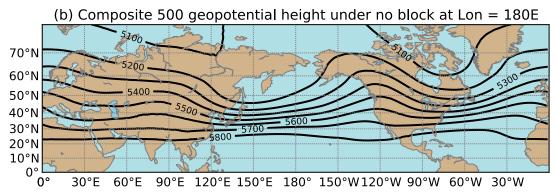
# 640 FIGURE CAPTIONS 641 642 **Figure 1:** Composite of Northern Hemisphere 500 hPa geopotential height patterns 643 under (a) blocked flow at 180° E longitude, and (b) unblocked flow at 180° E 644 longitude. 645 Figure 2: (a) Blocking frequency as determined from analyses and reforecasts as a 646 function of forecast lead time. Areas shaded in gray denote the two sectors in 647 subsequent figures, the Pacific and Euro-Atlantic sectors. (b) Analyzed, spatially 648 smoothed yearly blocking frequencies for each year between 1985 and 2012. 649 **Figure 3**: Brier Skill Scores of blocking probability forecasts for (a) Pacific, and (b) 650 Euro-Atlantic sectors. 651 **Figure 4**: As in Fig. 3, but for Brier Skill Scores of blocking probability forecasts by 652 half decade for (a) Pacific, and (b) Euro-Atlantic sectors. Solid lines present the skill 653 scores for the actual reforecasts, dashed lines present the skill under perfect-model 654 assumptions. 655 **Figure 5**: Reliability diagrams for blocking probability forecasts for (a) +3 day 656 forecast, (b) +6 day forecast, (c) +9 day forecast, (d) +12 day forecast, and (e) +15day forecast. Dotted red line denotes the skill in the Euro-Atlantic sector and dotted 657 658 blue line denotes the skill in the Pacific sector. Red and blue bars indicate the 659 frequency of usage of each forecast probability category for the Euro-Atlantic and 660 Pacific sectors, respectively. 661 **Figure 6**: RMM1 and RMM2 phase plots for (a) analyzed, and (b) control forecasts 662 whose initial states are within the purple circle. Differences in time from the initial

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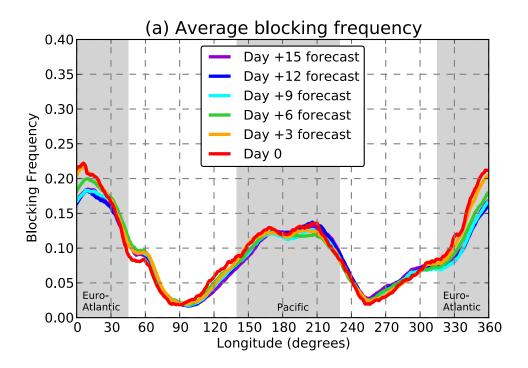
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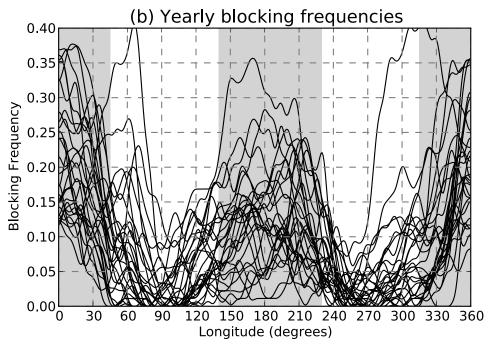
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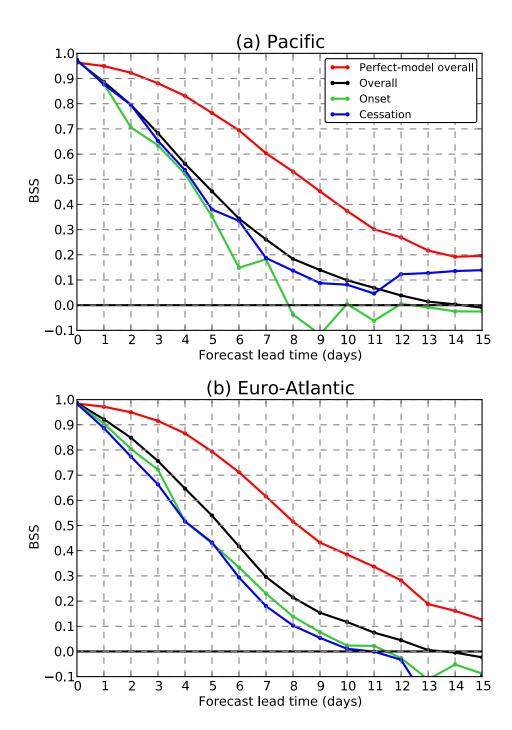


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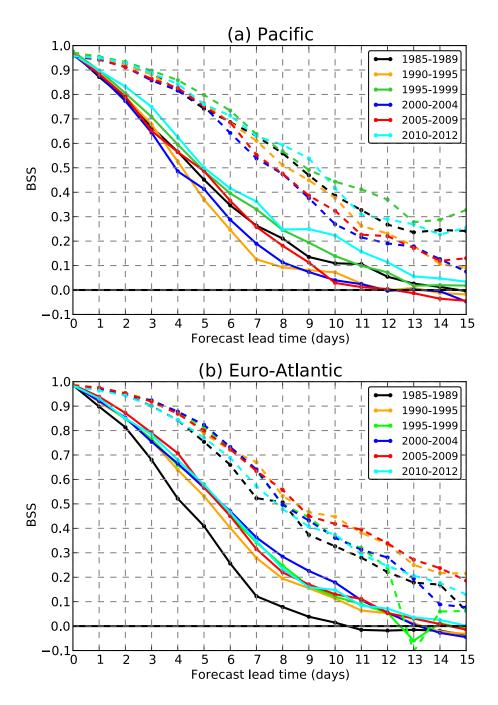




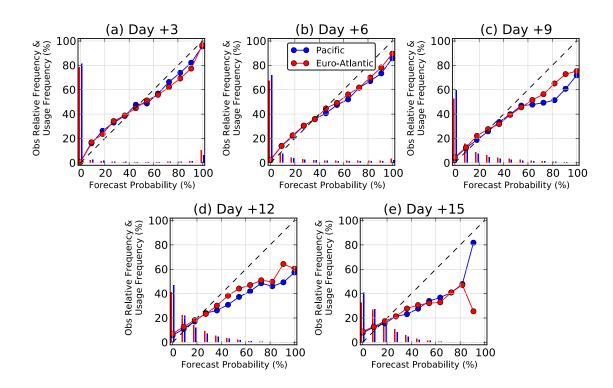
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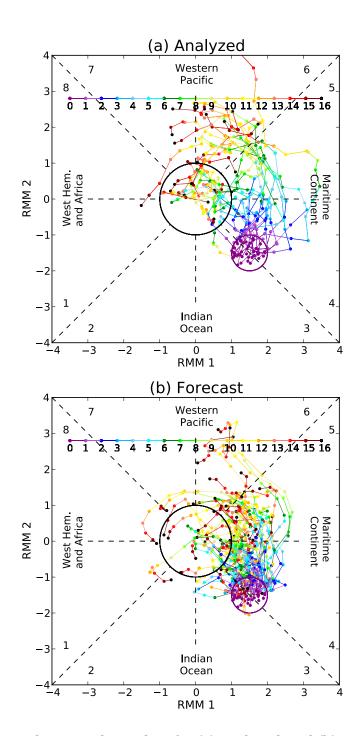
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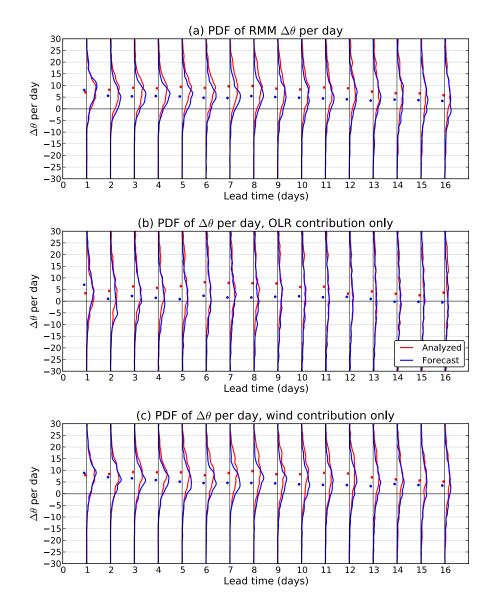
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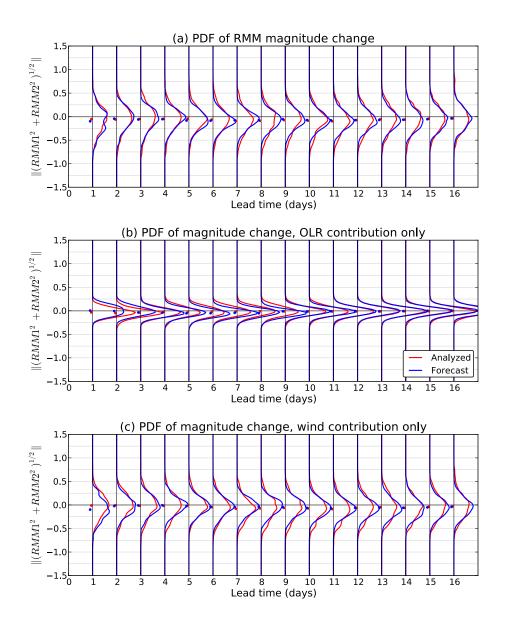
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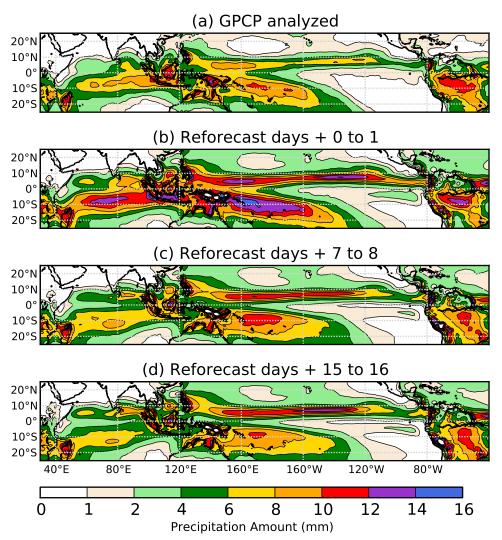
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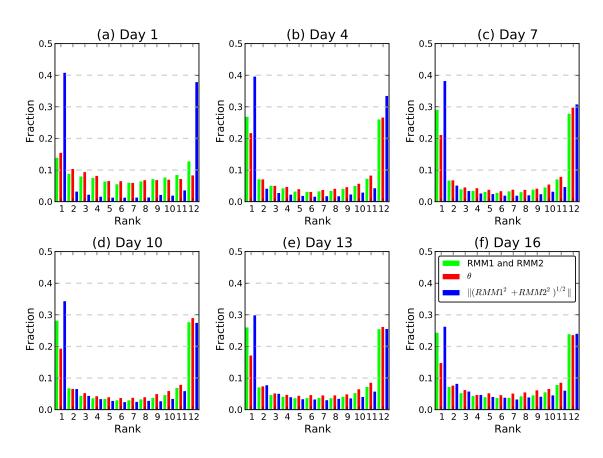
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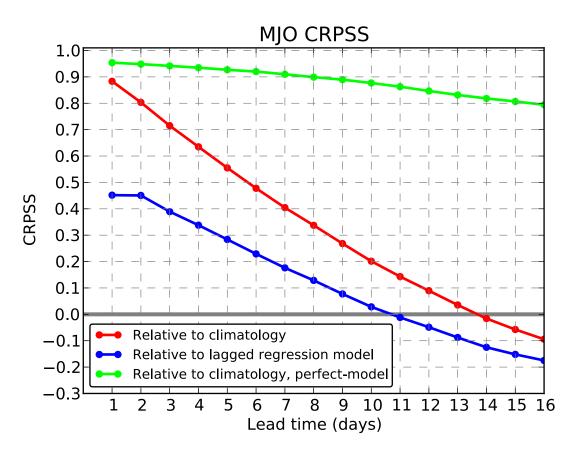
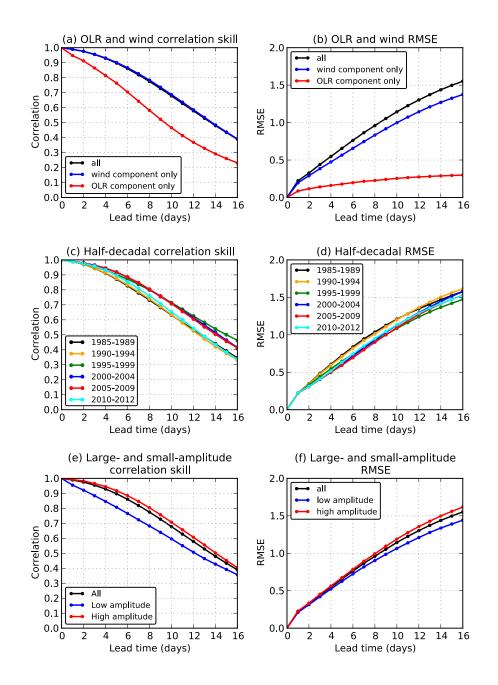
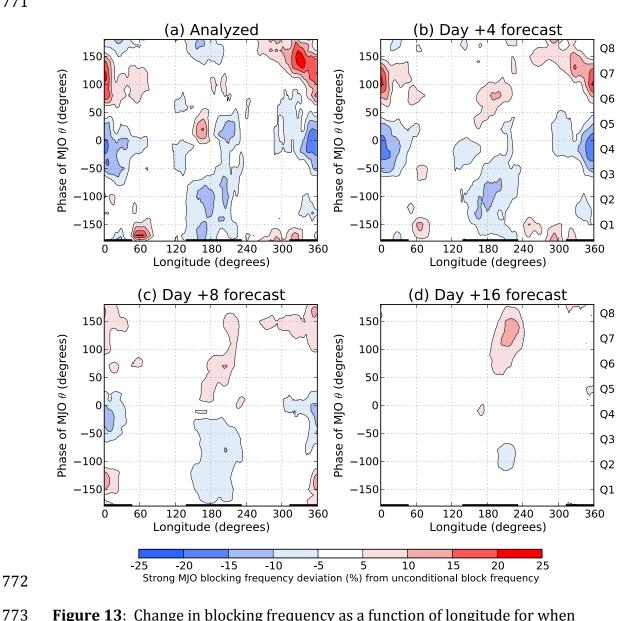


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